

# Lecture 12

# Network Tuning

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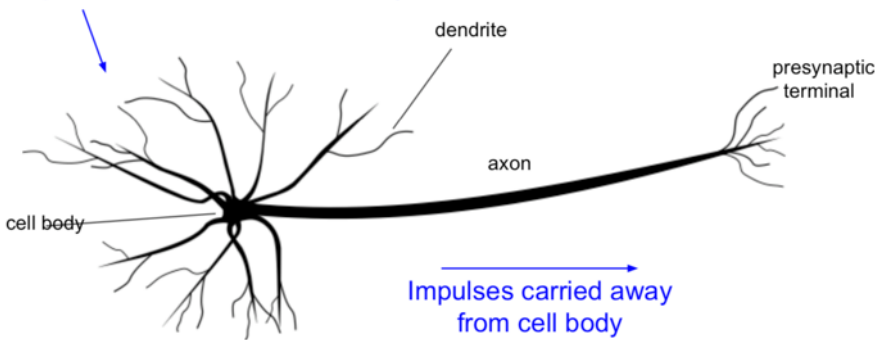
[Slides adapted from CS213n by Fei-Fei Li & CS230 by Andrew Ng @ Stanford.]

[Slides adapted from Tensorflow and deep learning without a PhD series by Martin Gorner @ Google.]

# Neural Network

## Biological Inspiration

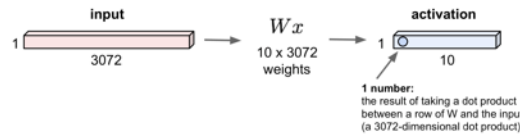
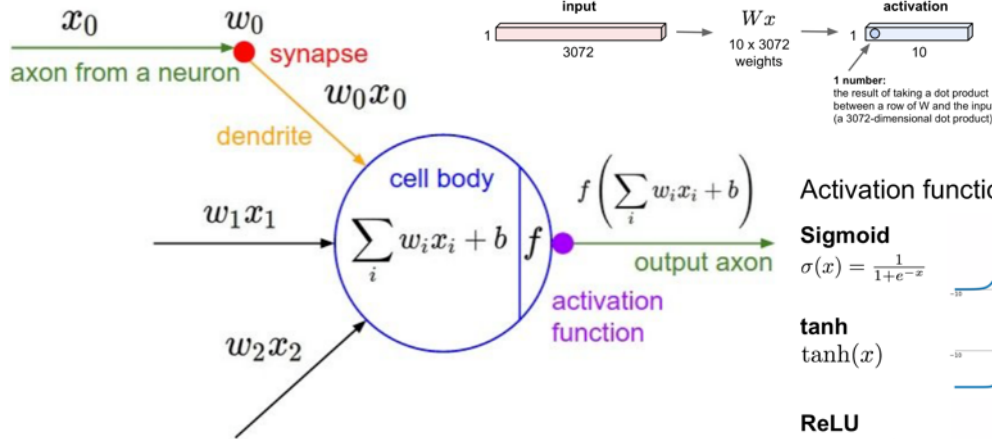
Impulses carried toward cell body



This image by Felipe Peruchio is licensed under CC-BY 3.0

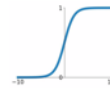
### Fully Connected Layer

32x32x3 image -> stretch to 3072 x 1

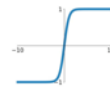


### Activation functions

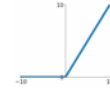
**Sigmoid**  
 $\sigma(x) = \frac{1}{1+e^{-x}}$



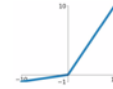
**tanh**  
 $\tanh(x)$



**ReLU**  
 $\max(0, x)$

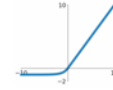


**Leaky ReLU**  
 $\max(0.1x, x)$



**Maxout**  
 $\max(w_1^T x + b_1, w_2^T x + b_2)$

**ELU**  
 $\begin{cases} x & x \geq 0 \\ \alpha(e^x - 1) & x < 0 \end{cases}$

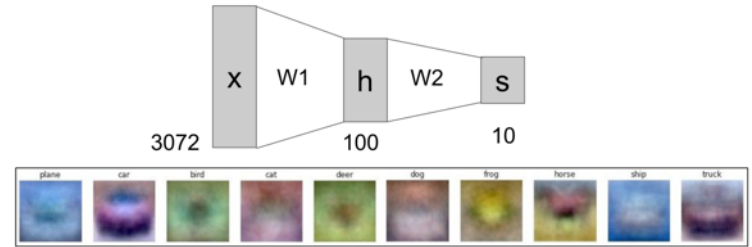


Linear score function:

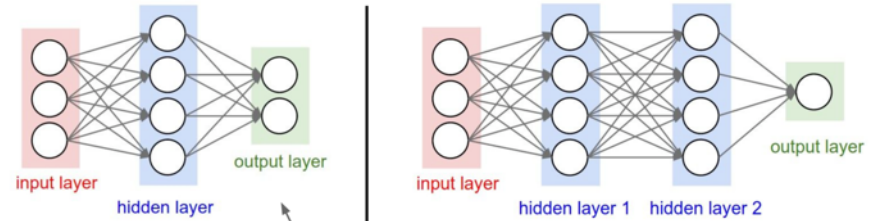
$$f = Wx$$

2-layer Neural Network

$$f = W_2 \max(0, W_1 x)$$



### Neural networks: Architectures



"2-layer Neural Net", or  
 "1-hidden-layer Neural Net"

"Fully-connected" layers

"3-layer Neural Net", or  
 "2-hidden-layer Neural Net"

```
# forward-pass of a 3-layer neural network:
f = lambda x: 1.0/(1.0 + np.exp(-x)) # activation function (use sigmoid)
x = np.random.randn(3, 1) # random input vector of three numbers (3x1)
h1 = f(np.dot(W1, x) + b1) # calculate first hidden layer activations (4x1)
h2 = f(np.dot(W2, h1) + b2) # calculate second hidden layer activations (4x1)
out = np.dot(W3, h2) + b3 # output neuron (1x1)
```



# [ConvNetJS demo: training on CIFAR-10]

<https://cs.stanford.edu/people/karpathy/convnetjs/demo/cifar10.html>

## ConvNetJS CIFAR-10 demo

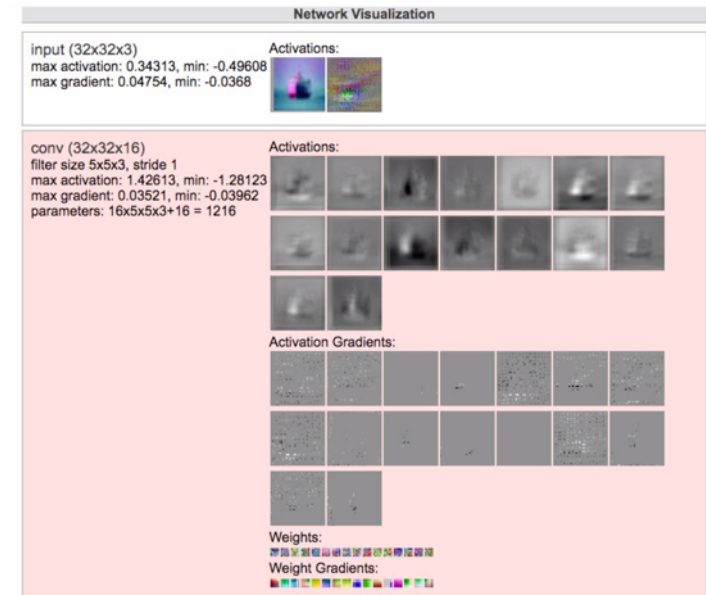
### Description

This demo trains a Convolutional Neural Network on the [CIFAR-10 dataset](#) in your browser, with nothing but Javascript. The state of the art on this dataset is about 90% accuracy and human performance is at about 94% (not perfect as the dataset can be a bit ambiguous). I used [this python script](#) to parse the [original files](#) (python version) into batches of images that can be easily loaded into page DOM with img tags.

This dataset is more difficult and it takes longer to train a network. Data augmentation includes random flipping and random image shifts by up to 2px horizontally and vertically.

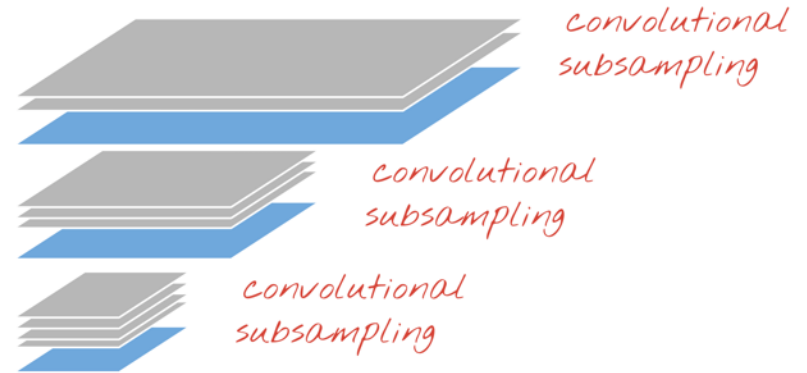
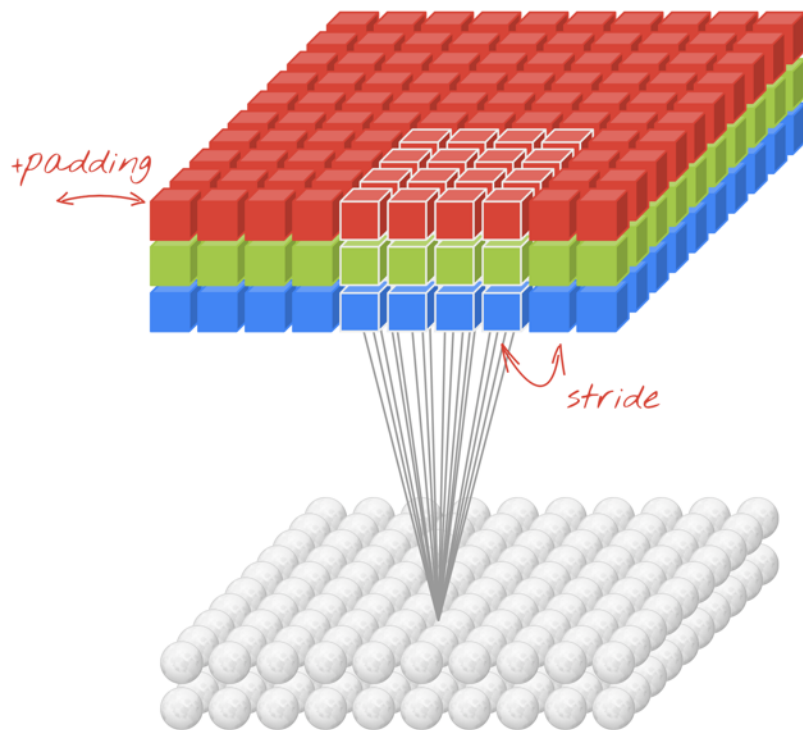
By default, in this demo we're using Adadelta which is one of per-parameter adaptive step size methods, so we don't have to worry about changing learning rates or momentum over time. However, I still included the text fields for changing these if you'd like to play around with SGD+Momentum trainer.

Report questions/bugs/suggestions to [@karpathy](#).



# Construct of a Convolutional Layer

## Convolutional layer

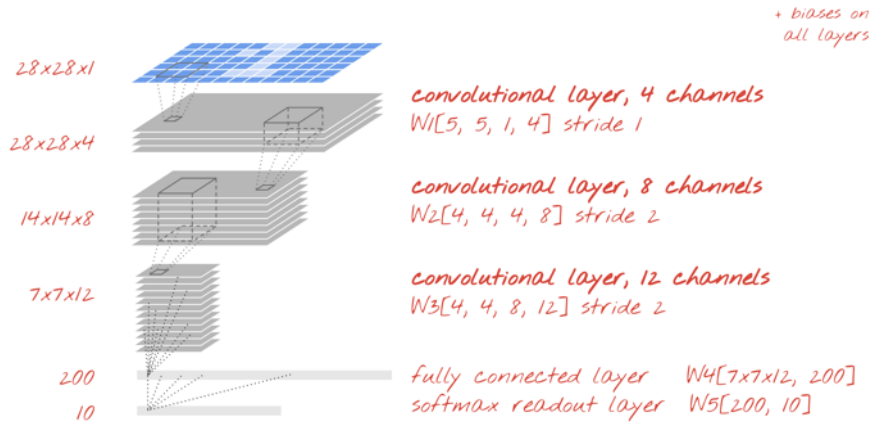


$$\left. \begin{array}{l} W_1[4, 4, 3] \\ W_2[4, 4, 3] \end{array} \right\} W[4, 4, 3, 2]$$

filter size      input channels      output channels

# python mnist\_3.0\_convolutional.py => 98.91%

## Convolutional neural network



## Tensorflow - initialisation

```

K=4
L=8
M=12

W1 = tf.Variable(tf.truncated_normal([5, 5, 1, K], stddev=0.1))
B1 = tf.Variable(tf.ones([K])/10)
W2 = tf.Variable(tf.truncated_normal([5, 5, K, L], stddev=0.1))
B2 = tf.Variable(tf.ones([L])/10)
W3 = tf.Variable(tf.truncated_normal([4, 4, L, M], stddev=0.1))
B3 = tf.Variable(tf.ones([M])/10)

N=200

W4 = tf.Variable(tf.truncated_normal([7*7*M, N], stddev=0.1))
B4 = tf.Variable(tf.ones([N])/10)
W5 = tf.Variable(tf.truncated_normal([N, 10], stddev=0.1))
B5 = tf.Variable(tf.zeros([10])/10)
    
```

*filter size* (points to 5, 5)  
*input channels* (points to 1)  
*output channels* (points to K)

*weights initialised with random values*

## Tensorflow - the model

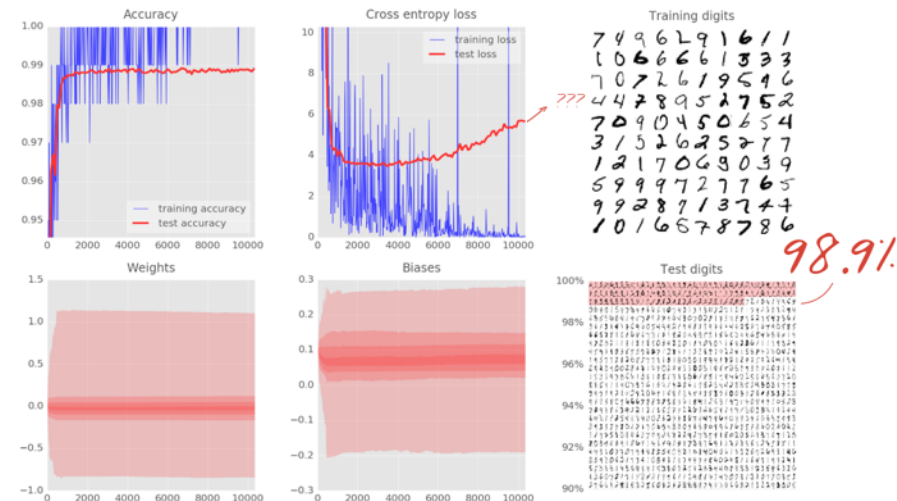
```

input image batch X[100, 28, 28, 1]
weights
stride
biases

Y1 = tf.nn.relu(tf.nn.conv2d(X, W1, strides=[1, 1, 1, 1], padding='SAME') + B1)
Y2 = tf.nn.relu(tf.nn.conv2d(Y1, W2, strides=[1, 2, 2, 1], padding='SAME') + B2)
Y3 = tf.nn.relu(tf.nn.conv2d(Y2, W3, strides=[1, 2, 2, 1], padding='SAME') + B3)

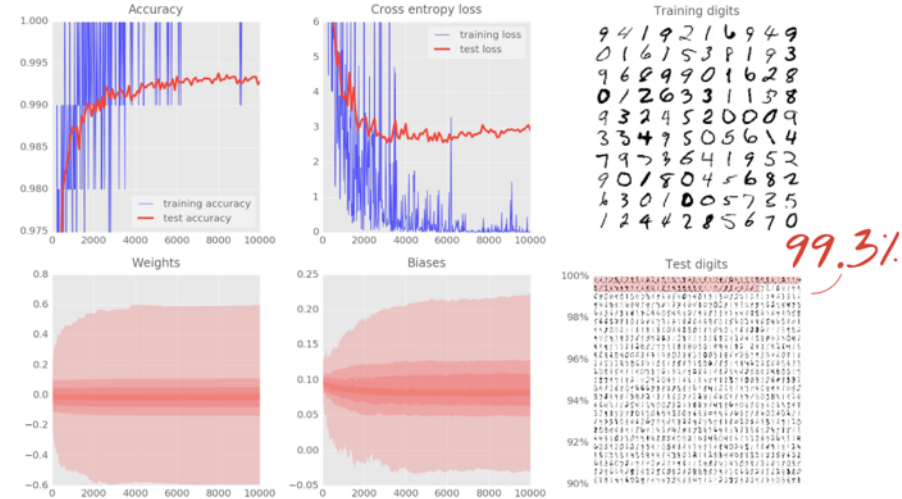
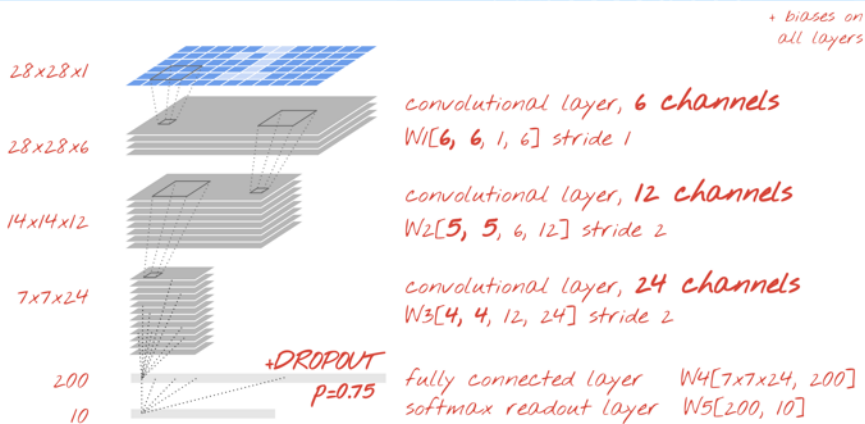
YY = tf.reshape(Y3, shape=[-1, 7 * 7 * M])
flatten all values for fully connected layer
Y3 [100, 7, 7, 12]
YY [100, 7*7*12]

Y4 = tf.nn.relu(tf.matmul(YY, W4) + B4)
Y = tf.nn.softmax(tf.matmul(Y4, W5) + B5)
    
```



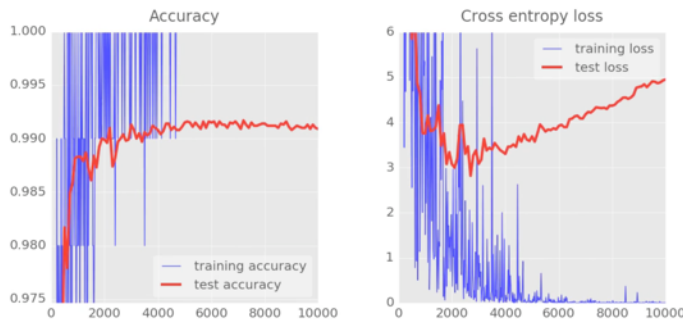
# python mnist\_3.1\_convolutional\_bigger\_dropout.py => 99.3%

## Bigger convolutional network + dropout



YEAH !

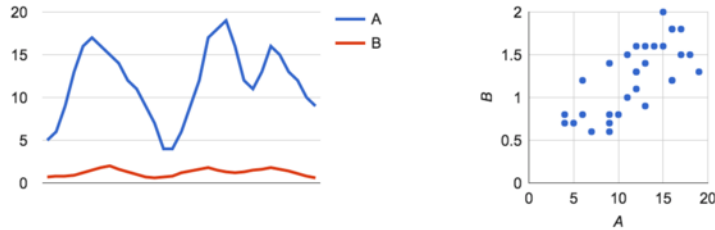
YEAH !



*with dropout*

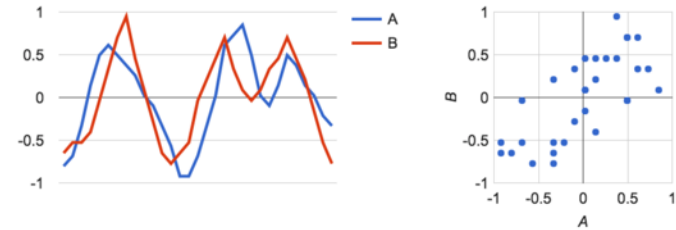
# Data Preprocessing

## Data "whitening"



Data: large values, different scales, skewed, correlated

## Data "whitening"



Modified data: centered around zero, rescaled...

*Subtract average  
Divide by std dev*

## Data "whitening"

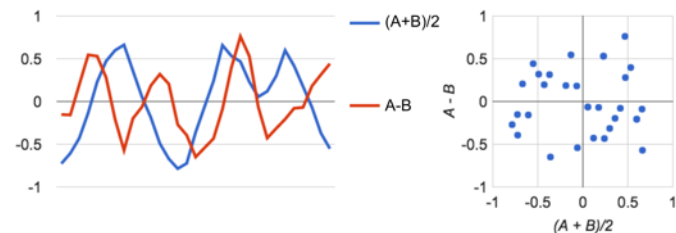
$$\begin{bmatrix} \text{new} \\ A \end{bmatrix} \quad \begin{bmatrix} \text{new} \\ B \end{bmatrix} = \begin{bmatrix} A & B \end{bmatrix} \times \begin{bmatrix} 0.05 & 0.12 \\ 0.61 & -1.23 \end{bmatrix} + \begin{bmatrix} -1.45 & 0.12 \end{bmatrix}$$

*Scale & rotate*      *shift*

*W?*      *B?*

*A network layer can do this!*

## Data "whitening"

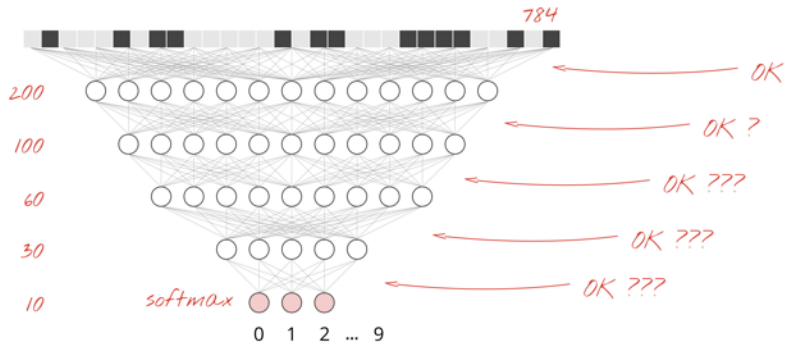


Modified data: ... and decorrelated (that was almost a Principal Component Analysis)

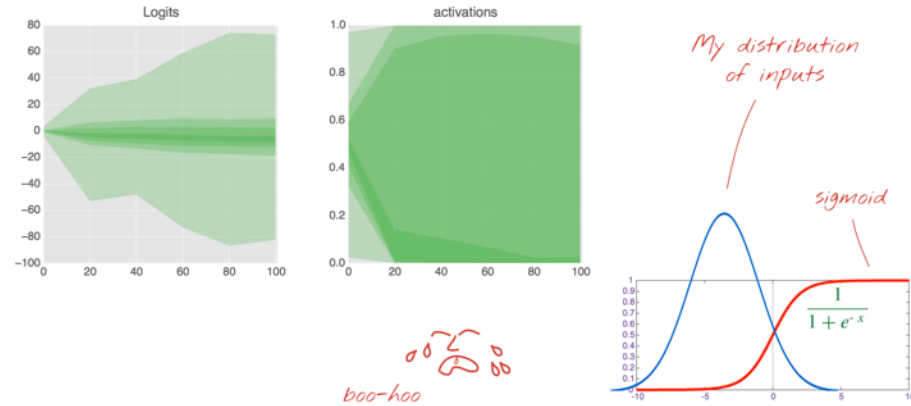


# Batch Normalization Theory

## Fully connected network



## Without batch normalisation



## Batch normalisation

Lightbulb icon: Compute average and variance on mini-batch

"logit" = weighted sum + bias

Lightbulb icon: Center and re-scale logits before the activation function (decorrelate? no, too complex)

$$\hat{x} = \frac{x - \text{avg}_{\text{batch}}(x)}{\text{stdev}_{\text{batch}}(x) + \epsilon}$$

Lightbulb icon: Add learnable scale and offset for each logit so as to restore expressiveness

one of each per neuron

$$BN(x) = \alpha \hat{x} + \beta$$

Try  $\alpha = \text{stdev}(x)$  and  $\beta = \text{avg}(x)$  and you have  $BN(x) = x$

## Batch normalisation

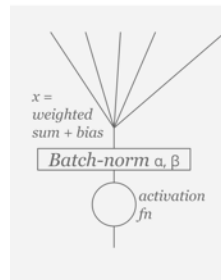
depends from: weights, biases, images

depends from: same weights and biases, images only one set of weights and biases in a mini-batch

$$\hat{x} = \frac{x - \text{avg}_{\text{batch}}(x)}{\text{stdev}_{\text{batch}}(x) + \epsilon}$$

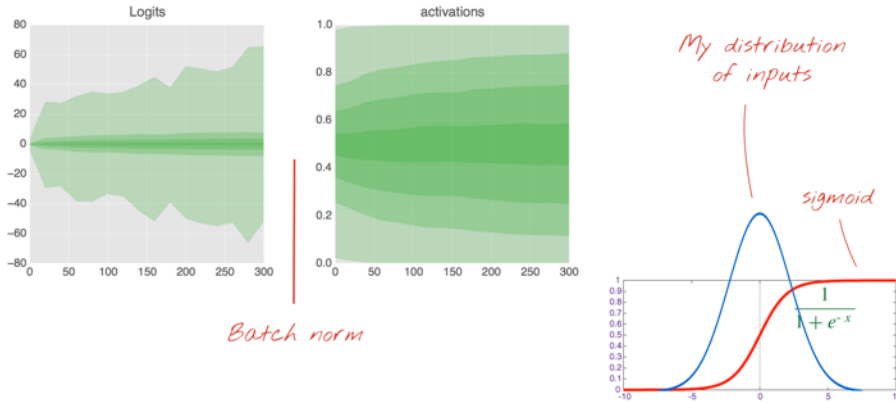
$$BN(x) = \alpha \hat{x} + \beta$$

=> BN is differentiable relatively to weights, biases,  $\alpha$  and  $\beta$   
It can be used as a layer in the network, gradient calculations will still work

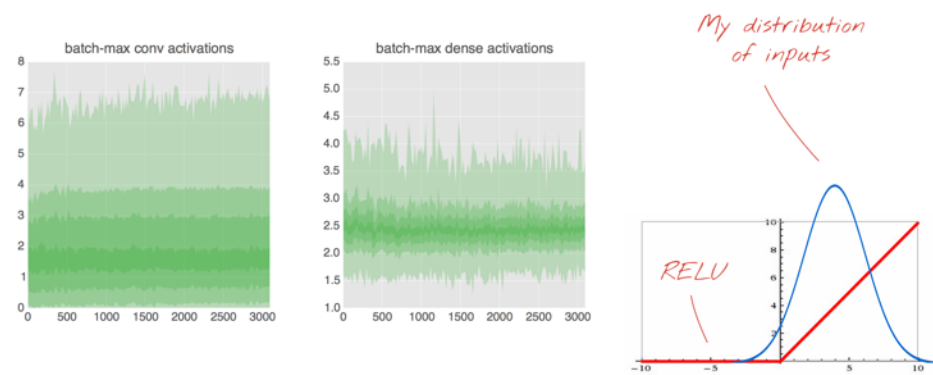


# Batch Normalization Done Right

With batch normalisation (sigmoid)



With batch normalisation (RELU)



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DEVON

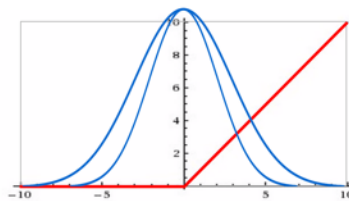
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Batch normalisation done right

biases :  
no longer useful

Per neuron:	relu	sigmoid
without BN	<b>bias</b>	<b>bias</b>
With BN	<b><math>\beta</math></b>	<b><math>\alpha, \beta</math></b>



+You can go faster: use higher learning rate  
+BN also regularises: lower or remove dropout



Usually inserted after Fully Connected or Convolutional layers, and before nonlinearity.

$$\hat{x}^{(k)} = \frac{x^{(k)} - E[x^{(k)}]}{\sqrt{\text{Var}[x^{(k)}]}}$$

**Input:** Values of  $x$  over a mini-batch:  $\mathcal{B} = \{x_1 \dots x_m\}$ ;  
Parameters to be learned:  $\gamma, \beta$

**Output:**  $\{y_i = \text{BN}_{\gamma, \beta}(x_i)\}$

$$\mu_{\mathcal{B}} \leftarrow \frac{1}{m} \sum_{i=1}^m x_i \quad // \text{ mini-batch mean}$$

$$\sigma_{\mathcal{B}}^2 \leftarrow \frac{1}{m} \sum_{i=1}^m (x_i - \mu_{\mathcal{B}})^2 \quad // \text{ mini-batch variance}$$

$$\hat{x}_i \leftarrow \frac{x_i - \mu_{\mathcal{B}}}{\sqrt{\sigma_{\mathcal{B}}^2 + \epsilon}} \quad // \text{ normalize}$$

$$y_i \leftarrow \gamma \hat{x}_i + \beta \equiv \text{BN}_{\gamma, \beta}(x_i) \quad // \text{ scale and shift}$$

- Improves gradient flow through the network
- Allows higher learning rates
- Reduces the strong dependence on initialization
- Acts as a form of regularization in a funny way, and slightly reduces the need for dropout, maybe

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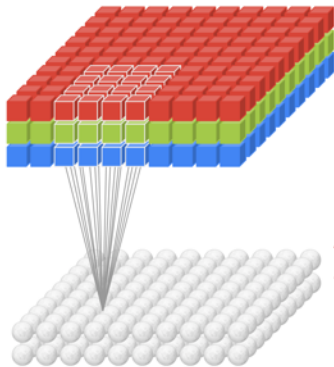


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of Science and Technology

# Convolutional Batch Normalization

## Convolutional batch normalisation

## Batch normalisation at test time



Each neuron or patch has a value:

- per image in the batch
- per x position
- per y position

=> compute avg and stdev across all  
batchsize x width x height values

$W_1[4, 4, 3] \rightarrow b_1, \alpha_1, \beta_1$  Still, one bias,  
scale or offset  
per neuron  
 $W_2[4, 4, 3] \rightarrow b_2, \alpha_2, \beta_2$

$$\hat{x} = \frac{x - avg?(x)}{stdev?(x) + \epsilon}$$

Stats on what ?

- Last batch: no
- all images: yes (but not practical)
- => Exponential moving average during training

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## Batch normalisation with Tensorflow

Define one offset and/or  
scale per neuron

```
def batchnorm_layer(Ylogits, is_test, Offset, Scale, iteration, convolutional=False):
```

```
    exp_moving_avg = tf.train.ExponentialMovingAverage(0.9999, iteration)
```

```
    if convolutional: # avg across batch, width, height
```

```
        mean, variance = tf.nn.moments(Ylogits, [0, 1, 2])
```

```
    else:
```

```
        mean, variance = tf.nn.moments(Ylogits, [0])
```

```
    update_moving_averages = exp_moving_avg.apply([mean, variance])
```

```
    m = tf.cond(is_test, lambda: exp_moving_avg.average(mean), lambda: mean)
```

```
    v = tf.cond(is_test, lambda: exp_moving_avg.average(variance), lambda: variance)
```

```
    Ybn = tf.nn.batch_normalization(Ylogits, m, v, Offset, Scale, variance_epsilon=1e-5)
```

```
    return Ybn, update_moving_averages
```

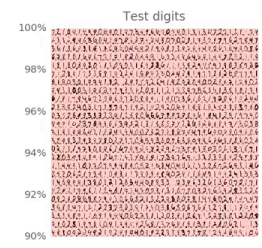
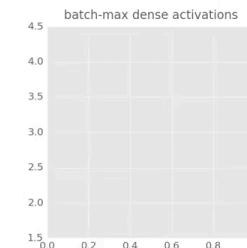
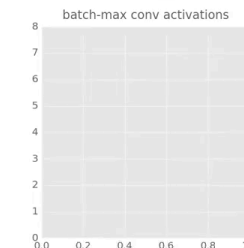
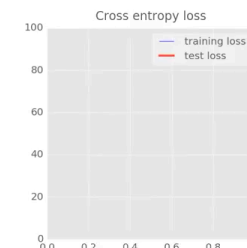
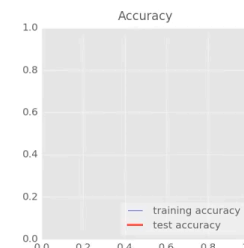
don't forget to execute this (sess.run)  
apply activation fn on Ybn

DEVONX

The code is on GitHub: [https://github.com/martin\\_gorner/DEVONX](https://github.com/martin_gorner/DEVONX)

Google CloudPlatform

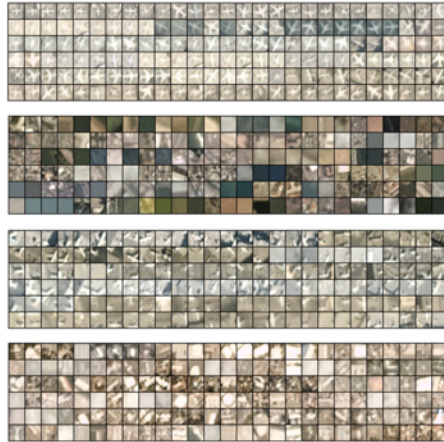
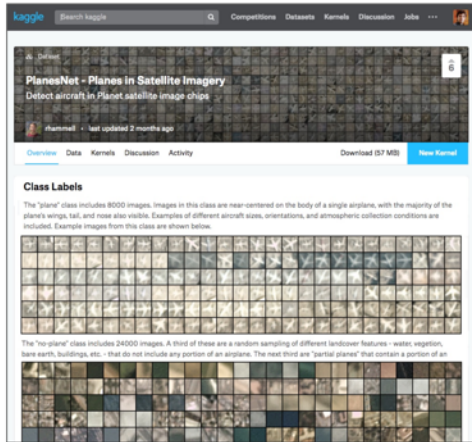
AncoraSIR.com



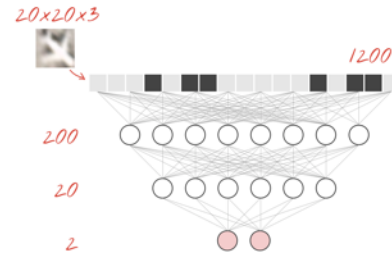
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# Example: Airplane or not?

## Kaggle



## Fully-connected layers



```

X = tf.reshape(images, [-1, 20*20*3])
Y1 = tf.layers.dense(X, 200,
                    activation=tf.nn.relu)
Y2 = tf.layers.dense(Y1, 20,
                    activation=tf.nn.relu)
Ylogits = tf.layers.dense(Y2, 2)
    
```

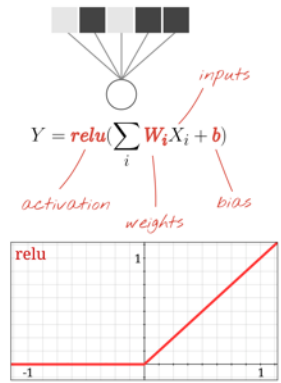
```

loss = tf.losses.softmax_cross_entropy(tf.one_hot(is_plane,2), Ylogits)
train_op = tf.train.AdamOptimizer(0.001).minimize(loss)
    
```

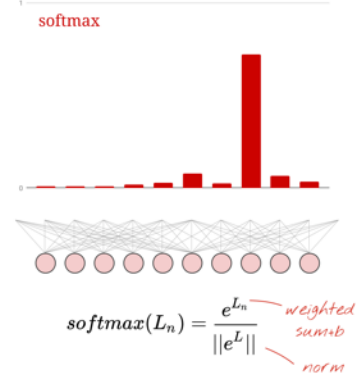
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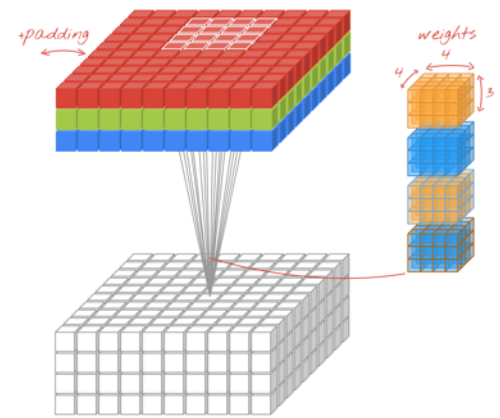
## Activation functions



Classification head  
Hidden layers



## Convolutional layer



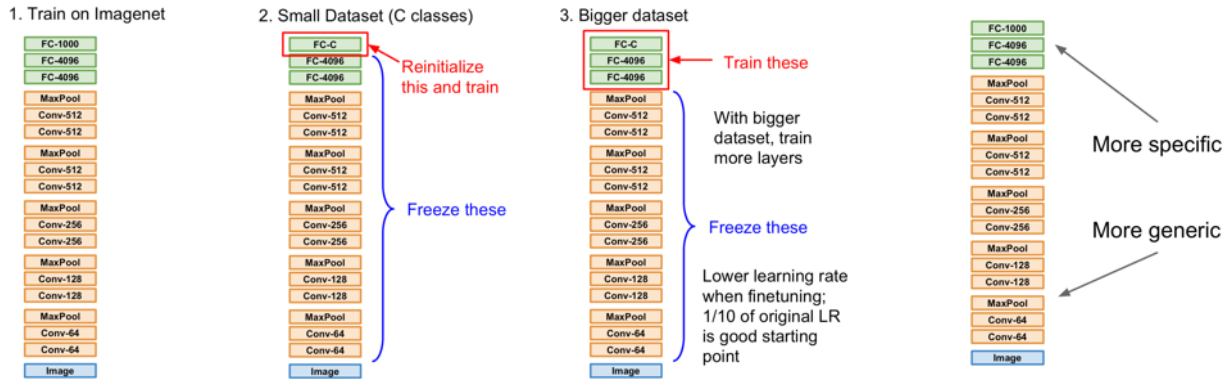
$W[4, 4, 3, 4]$   
filter size input channels nb of filters = output channels

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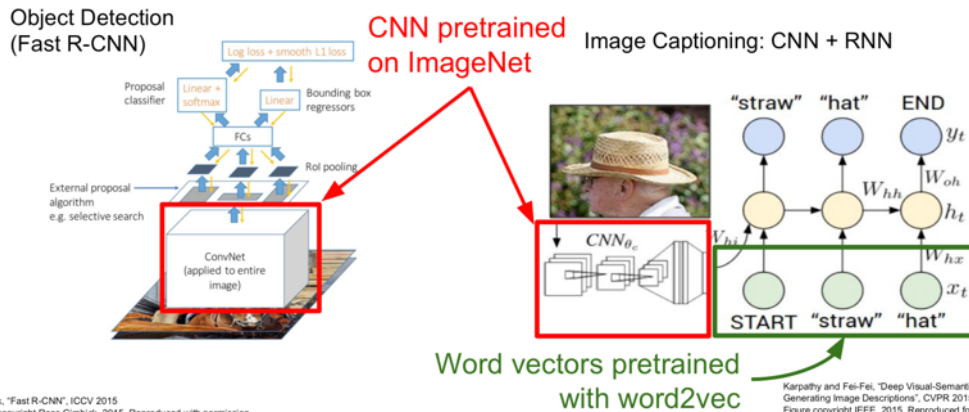
# Transfer Learning

You need a lot of data if you want to train/use CNNs, **really?**



	very similar dataset	very different dataset
very little data	Use Linear Classifier on top layer	You're in trouble... Try linear classifier from different stages
quite a lot of data	Finetune a few layers	Finetune a larger number of layers

Transfer learning with CNNs is pervasive...  
(it's the norm, not an exception)



Next class:

- Transfer learning for arcade claw machine robot

Girshick, "Fast R-CNN", ICCV 2015. Figure copyright Ross Girshick, 2015. Reproduced with permission.

Karpathy and Fei-Fei, "Deep Visual-Semantic Alignments for Generating Image Descriptions", CVPR 2015. Figure copyright: IEEE, 2015. Reproduced for educational purposes.

# Thank you!

Prof. Song Chaoyang

- Dr. Wan Fang ([sophie.fwan@hotmail.com](mailto:sophie.fwan@hotmail.com))

